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**The Resonances of the Capelli Operators for Small Split Orthosymplectic Dual Pairs**

Let  $(G, G')$  be a reductive dual pair in  $\mathrm{Sp}(W)$  with  $\mathrm{rank} G \leq \mathrm{rank} G'$  and  $G'$  semisimple. The image of the Casimir element of the universal enveloping algebra of  $G'$  under the Weil representation  $\omega$  is a Capelli operator. It is a hermitian operator acting on the smooth vectors of the representation space of  $\omega$ . We compute the resonances of a natural multiple of a translation of this operator for small split orthosymplectic dual pairs. The corresponding resonance representations turn out to be  $GG'$ -modules in Howe's correspondence. We determine them explicitly.

**Keywords:** Resonances, Capelli operators, Howe's correspondence.

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