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**Biderivations and Commuting Linear Maps on Lie Algebras**

Let  $L$  be a Lie algebra over a commutative unital ring  $F$  containing  $\frac{1}{2}$ . If  $L$  is perfect and centerless, then every skew-symmetric biderivation  $\delta: L \times L \rightarrow L$  is of the form  $\delta(x, y) = \gamma([x, y])$  for all  $x, y \in L$ , where  $\gamma \in \text{Cent}(L)$ , the centroid of  $L$ . Under a milder assumption that  $[c, [L, L]] = \{0\}$  implies  $c = 0$ , every commuting linear map from  $L$  to  $L$  lies in  $\text{Cent}(L)$ . These two results are special cases of our main theorems which concern biderivations and commuting linear maps having their ranges in an  $L$ -module. We provide a variety of examples, some of them showing the necessity of our assumptions and some of them showing that our results cover several results from the literature.

**Keywords:** Lie algebra, biderivation, commuting linear map, centroid.

**MSC:** 17B05, 17B40, 16R60.