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Journal of Lie Theory 27 (2017) 397–417

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### **A Distributional Treatment of Relative Mirabolic Multiplicity One**

We study the role of the mirabolic subgroup  $P$  of  $G = \mathbf{GL}_n(F)$  ( $F$  a  $p$ -adic field) for smooth irreducible representations of  $G$  that are distinguished relative to a subgroup of the form  $H_k = \mathbf{GL}_k(F) \times \mathbf{GL}_{n-k}(F)$ . We show that if a non-zero  $H_1$ -invariant linear form exists on a representation, then the a priori larger space of  $P \cap H_1$ -invariant forms is one-dimensional. When  $k > 1$ , we give a reduction of the same problem to a question about invariant distributions on the nilpotent cone tangent to the symmetric space  $G/H_k$ . Some new distributional methods for non-reductive groups are developed.

**Keywords:** Distinguished representations,  $p$ -adic symmetric spaces, mirabolic subgroup, invariant distributions.

**MSC:** 20G25, 22E50