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**On the Principal Bundles over a Flag Manifold**

Let  $P$  be a parabolic subgroup of a semisimple simply connected linear algebraic group  $G$  over  $\mathbb{C}$  and  $\rho$  an irreducible homomorphism from  $P$  to a complex reductive group  $H$ . We show that the associated principal  $H$ -bundle over  $G/P$ , associated for  $\rho$  to the principal  $P$ -bundle defined by the quotient map  $G \rightarrow G/P$ , is stable. We describe the Harder–Narasimhan reduction of the  $G$ -bundle over  $G/P$  obtained using the composition  $P \rightarrow L(P) \rightarrow G$ , where  $L(P)$  is the Levi factor of  $P$ .