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Coproximality in Spaces of Bochner Integrable Functions

In this short note we use a new way of applying von Neumann’s selection theorem for obtaining best coapproximation in spaces of measurable functions. For a coproximal closed subspace Y of a Banach space X , we show that if Y is constrained in a weakly compactly generated dual space, then the space $L^1(\mu, Y)$ of Y -valued Bochner integrable functions is coproximal in $L^1(\mu, X)$. This extends a result of M. R. Haddadi, N. Hejazjpoor and H. Mazaheri [*Some results about best coapproximation in $L^P(S, X)$* , Anal. Theory Appl. 26 (2010) 69–75], proved when Y is reflexive.

Keywords: Coproximality, constrained subspaces, weakly compactly generated spaces, spaces of Bochner integrable functions, von Neumann’s selection theorem.

MSC: 41A50; 46B20, 46E40