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**A. Amir**

University of Mostaganem, Faculty of Sciences, Dept. of Mathematics, 27000 Mostaganem,  
Algeria  
amir@univ-mosta.dz

**H. Mokhtar-Kharroubi**

University of Oran, Faculty of Sciences, Dept. of Mathematics, Oran, Algeria  
hmkharroubi@yahoo.fr

**Normality and Quasiconvex Integrands**

Let  $(T, \mathcal{A})$  be an arbitrary measurable space and  $f$  an integrand defined on  $T \times \mathbb{R}^n$  such that  $f(t, \cdot)$  is quasiconvex and lower semicontinuous. Here, convexity is present by the level set mapping. We show that the normality property of the integrand in the sense of R. T. Rockafellar [Pacific Journal of Mathematics 24 (1968) 525–539; and in: Nonlinear Operators and the Calculus of Variations; Bruxelles 1975, Lecture Notes in Mathematics 543, 157–207, Springer, Berlin] can be characterized by the normality of the level set mapping, and that normality is preserved for quasiconvex conjugates. Finally we obtain for the integral  $I_f(x(\cdot)) = \int_T f(t, x(t)) d\mu(t)$  the equality (in appropriate topology) between the lower semicontinuous regularization and the second quasiconvex conjugate.

**Keywords:** Normal integrand, quasiconvex functions, conjugation.

**MSC:** 26B25, 49N15, 49J53