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Journal of Convex Analysis 16 (2009) 523–541

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**Weak and Entropy Solutions to Nonlinear Elliptic Problems with Variable Exponent**

We study the boundary value problem  $-div(a(x, \nabla u)) = f(x, u)$  in  $\Omega$ ,  $u = 0$  on  $\partial\Omega$ , where  $\Omega$  is a smooth bounded domain in  $\mathbb{R}^N$  and  $div(a(x, \nabla u))$  is a  $p(x)$ -Laplace type operator. We obtain the existence and uniqueness of an entropy solution for  $L^1$ -data  $f$  independent of  $u$ , the existence of weak energy solution for general data  $f$  dependent of  $u$  where the variable exponent  $p(\cdot)$  is not necessarily continuous.

**Keywords:** Generalized Lebesgue-Sobolev spaces, weak energy solution, entropy solution,  $p(x)$ -Laplace operator, electrorheological fluids.