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### **Representation of Viscosity Solutions of Hamilton-Jacobi Equations**

Hamilton Jacobi equations of the form  $H(x, u, Du) = 0$  are considered with  $H(x, r, p)$  nondecreasing in  $r$  and quasiconvex in  $p$ . A viscosity solution may be represented as the value function of a calculus of variations or control problem in  $L^\infty$ , i.e., as a minimax problem. For time dependent problems of the form  $u_t + H(t, x, u, Du) = 0$  we require that  $H(t, x, r, p)$  is convex in  $p$  and nondecreasing in  $r$ . The viscosity solution is then given as the value of an  $L^\infty$  problem.

**Keywords:** Quasiconvex, Hamilton-Jacobi, representation.

**MSC:** 35F21, 49L25