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### **Characters of the Nullcone Related to Vinberg Groups**

Let  $G$  be a reductive linear algebraic group defined over an algebraically closed field  $k$  of characteristic 0, and let  $\theta$  be an automorphism of  $G$  of order  $m$ . We consider the Vinberg pair  $(G_0, \mathfrak{g}_1)$ , where  $G_0$  is the identity component of the subgroup  $G^\theta$  of  $\theta$ -fixed points in  $G$  and  $\mathfrak{g}_1$  is the  $\omega$ -eigenspace of  $d\theta$  in  $\mathfrak{g} = \text{Lie}(G)$ , where  $\omega$  is a primitive  $m$ th root of 1 in  $k$ . In particular, we derive a formula for the formal characters of the  $G_0$ -modules  $k_n[\mathcal{N}]$ , where  $\mathcal{N}$  is the variety of nilpotent elements in  $\mathfrak{g}_1$  and  $k_n[\mathcal{N}]$  is the space of polynomials on  $\mathcal{N}$  of homogeneous degree  $n$ . We use this formula to compute the multiplicities of the simple highest weight modules in  $k_n[\mathcal{N}]$ . This multiplicity formula is also shown to hold for all  $n$  up to a certain maximum when  $k$  has positive characteristic.

**Keywords:** Reductive groups, Vinberg pairs, nullcone, formal characters, good characteristic.

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