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Hypergeometric Functions and Hyperbolic Metric

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Abstract. We obtain new inequalities for certain hypergeometric functions. Using these inequalities, we deduce estimates for the hyperbolic metric and the induced distance function on a certain canonical hyperbolic plane domain.

Keywords. Hypergeometric functions, complete elliptic integrals, convexity, hyperbolic metric, Poincaré density.

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