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**Non-Tangential Limits
of Slowly Growing Analytic Functions**

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Abstract. We show that if f is an analytic function in the unit disc \mathbb{D} ,

$$M(r, f) = \mathcal{O}((1 - r)^{-\eta}) \quad \text{as } r \rightarrow 1, \quad \text{for every } \eta > 0,$$

and

$$\sup_{0 \leq r < 1} (1 - r)^s |f'(r\zeta)| < \infty, \quad \text{where } |\zeta| = 1, s < 1,$$

then f has a finite non-tangential limit at ζ . We also show that in this result it is not sufficient to assume that

$$M(r, f) = \mathcal{O}((1 - r)^{-\eta}) \quad \text{as } r \rightarrow 1, \quad \text{for some fixed } \eta > 0.$$

Keywords. Non-tangential limit, Fatou point, slowly growing analytic function.

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